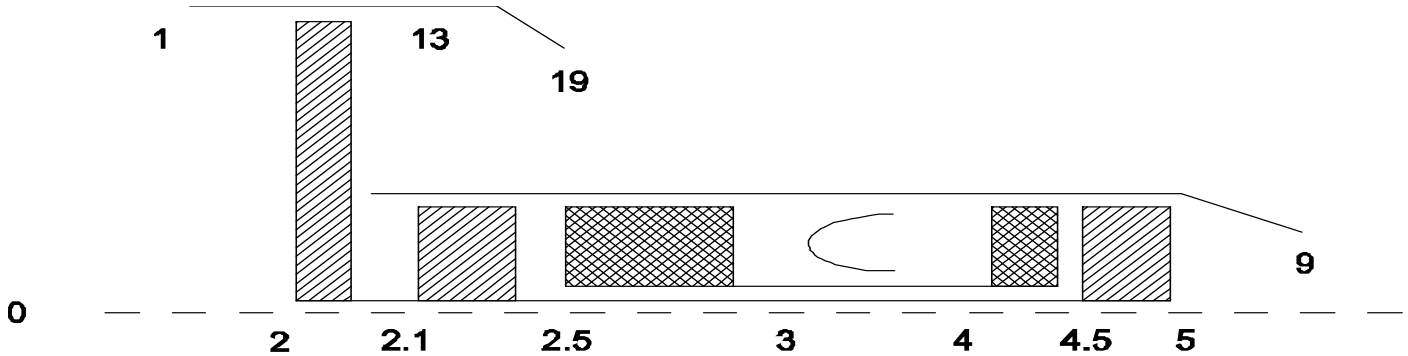


Turbofan de Correntes Separadas com Dois Eixos (“Twin-Spool”)

Diagrama Esquemático



Análise de Ciclo Não-Ideal

Dados de Entrada

Dados de voo

$$M_o [Mach], (P_o [Pa], T_o [K]) \text{ ou } H_o [m]$$

Dados do combustível e limite tecnológico da turbina

$$h_{PR} [J/kg], T_{t4} [K]$$

Dados dos fluidos de trabalho

$$\gamma, R [J/(kg \cdot K)], c_p [J/(kg \cdot K)]$$

ar (subscrito c)

$$\gamma_c = 1,4 \quad R_c = 287 J/(kg \cdot K)$$

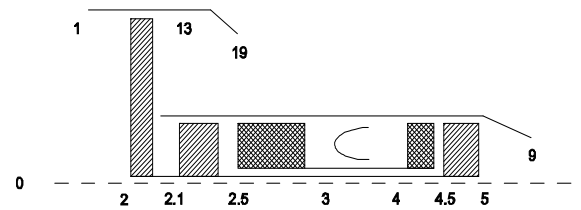
$$c_{pc} = 1004 J/(kg \cdot K)$$

gás queimado (subscrito t)

$$\gamma_t = 1,3 \quad R_t = 291 J/(kg \cdot K)$$

$$c_{pt} = 1100 J/(kg \cdot K)$$

Dados de componentes do motor



$$\pi_{dmax}, \pi_f, \pi_{cL}, \pi_{cH}, \pi_b, \eta_b, \pi_n$$

Escoamento livre (0), não perturbado (T_0, P_0, M_0)

Entrada de Ar (0-1)

$$\tau_r = 1 + \frac{\gamma - 1}{2} M_0^2 \quad \pi_r = \tau_r^{\frac{\gamma}{\gamma-1}}$$

Entrada de Ar (1-2), com eficiência de recuperação (η_r)

$$\eta_r = [1 - 0,075(M_0 - 1)^{1,35}]$$

para $M_0 > 1$

e $\eta_r = 1$ para $M_0 \leq 1$

$$\pi_d = \eta_r \pi_{dmax} \quad \tau_d = \pi_d^{\frac{\gamma_c - 1}{\gamma_c}}$$

Fan (2-2.1) e (2-13)

$$\tau_f = \pi_f^{\frac{\gamma_c - 1}{\gamma_c e_f}}$$

Compressor de baixa pressão (2.1-2.5)

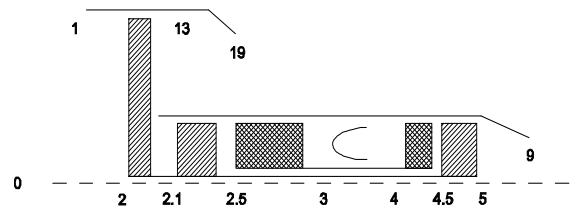
$$\tau_{cL} = \pi_{cL}^{\frac{\gamma_c - 1}{\gamma_c e_{cL}}} \quad \eta_{cL} = \frac{\pi_{cL}^{(\gamma_c - 1)/\gamma_c} - 1}{\tau_{cL} - 1}$$

Compressor de alta pressão (2.5-3)

$$\tau_{cH} = \pi_{cH}^{\frac{\gamma_c - 1}{\gamma_c e_{cH}}} \quad \eta_{cH} = \frac{\pi_{cH}^{(\gamma_c - 1)/\gamma_c} - 1}{\tau_{cH} - 1}$$

Combustor (3-4)

$$\tau_\lambda = \frac{c_{pt} T_{t4}}{c_{pc} T_0}$$



$$\eta_b \dot{m}_f h_{PR} = (\dot{m}_f + \dot{m}_C) c_{pt} T_{t4} - \dot{m}_C c_{pt} T_{t3}$$

$$f = \frac{\dot{m}_f}{\dot{m}_C} = \frac{\tau_\lambda - \tau_r \tau_d \tau_f \tau_{cL} \tau_{cH}}{\eta_b h_{PR} / (c_{pc} T_0) - \tau_\lambda}$$

Turbina de alta pressão (4-4.5)

$$\dot{m}_C c_{pc} (T_{t3} - T_{t2.5}) = -\eta_{mH} (\dot{m}_C + \dot{m}_f) c_{pt} (T_{t4.5} - T_{t4})$$

$$\tau_{tH} = 1 - \eta_{mH} \frac{(\tau_{cH} - 1) \tau_r \tau_d \tau_f \tau_{cL}}{(1 + f) \tau_\lambda}$$

$$\pi_{tH} = \tau_{tH}^{\gamma_t / (\gamma_t - 1)} e_{tH}$$

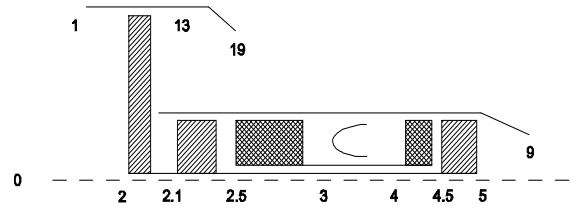
$$\eta_{tH} = \frac{\tau_{tH} - 1}{\pi_{tH}^{(\gamma_t - 1) / \gamma_t} - 1}$$

Turbina de baixa pressão (4.5-5)

$$[\dot{m}_F c_{pc} (T_{t13} - T_{t2}) - \dot{m}_C c_{pc} (T_{t2.5} - T_{t2})] = -\eta_{mL} (\dot{m}_C + \dot{m}_f) c_{pt} (T_{t5} - T_{t4.5})$$

$$\tau_{tL} = 1 - \eta_{mL} \frac{[\alpha (\tau_f - 1) + (\tau_{cL} - 1)] \tau_r \tau_d}{(1 + f) \tau_\lambda \tau_{tH}}$$

$$\alpha = \frac{\dot{m}_F}{\dot{m}_C}$$



$$\dot{m}_0 = \dot{m}_C + \dot{m}_F$$

$$\pi_{tL} = \tau_{tL} \gamma_t / (\gamma_t - 1) e_{tL}$$

$$\eta_{tL} = \frac{\tau_{tL} - 1}{\pi_{tL} (\gamma_t - 1) / \gamma_t - 1}$$

Tubeira do motor central (5-9)

Condição prescrita $\frac{P_0}{P_9}$

$$\frac{P_{t9}}{P_9} = \frac{P_0}{P_9} \pi_r \pi_d \pi_f \pi_{cL} \pi_{cH} \pi_b \pi_{tH} \pi_{tL} \pi_n$$

Condição subsônica $\frac{P_{t9}}{P_9} < \left(\frac{\gamma_t + 1}{2}\right)^{\gamma_t / (\gamma_t - 1)}$ $\frac{P_0}{P_9} = 1$

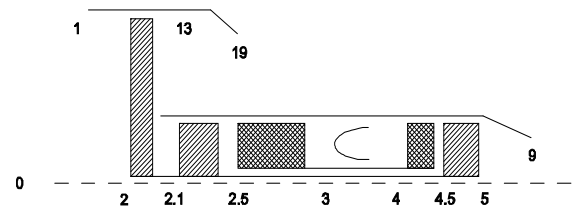
$$M_9 = \sqrt{\frac{2}{\gamma_t - 1} \left[\left(\frac{P_{t9}}{P_9}\right)^{(\gamma_t - 1) / \gamma_t} - 1 \right]}$$

$$\frac{T_{t9}}{T_0} = \frac{c_{pc}}{c_{pt}} \tau_\lambda \tau_{tH} \tau_{tL} \tau_n$$

$$\frac{T_9}{T_0} = \frac{T_{t9} / T_0}{(P_{t9} / P_9)^{(\gamma_t - 1) / \gamma_t}}$$

$$\frac{V_9}{a_0} = M_9 \sqrt{\frac{\gamma_t R_t T_9}{\gamma_c R_c T_0}}$$

Tubeira do fan (13-19)



Condição subsônica $\frac{P_{t19}}{P_{19}} < \left(\frac{\gamma_c+1}{2}\right)^{\gamma_c/(\gamma_c-1)} \quad \frac{P_0}{P_{19}} = 1$

$$\frac{P_{t19}}{P_{19}} = \frac{P_0}{P_{19}} \pi_r \pi_d \pi_f \pi_{fn}$$

$$M_{19} = \sqrt{\frac{2}{\gamma_c - 1} \left[\left(\frac{P_{t19}}{P_{19}}\right)^{(\gamma_c-1)/\gamma_c} - 1 \right]}$$

$$\frac{T_{t19}}{T_0} = \tau_r \tau_f \tau_{fn}$$

$$\frac{T_{19}}{T_0} = \frac{T_{t19}/T_0}{(P_{t19}/P_{19})^{(\gamma_c-1)/\gamma_c}}$$

$$\frac{V_{19}}{a_0} = M_{19} \sqrt{\frac{T_{19}}{T_0}}$$

Empuxo específico

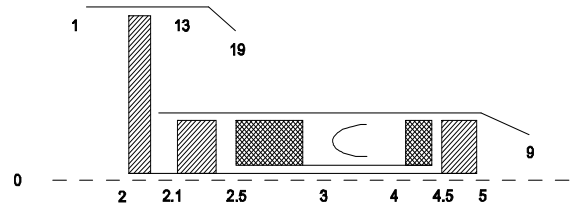
$$\frac{F_C}{\dot{m}_0} = \frac{a_0}{(1 + \alpha)} \left[(1 + f) \frac{V_9}{a_0} - M_0 + (1 + f) \frac{R_t T_9/T_0 (1 - P_0/P_9)}{R_c V_9/a_0 \gamma_c} \right]$$

$$\frac{F_F}{\dot{m}_0} = \frac{\alpha a_0}{(1 + \alpha)} \left[\frac{V_{19}}{a_0} - M_0 + \frac{T_{19}/T_0 (1 - P_0/P_{19})}{V_{19}/a_0 \gamma_c} \right]$$

$$\frac{F}{\dot{m}_0} = \frac{F_C}{\dot{m}_0} + \frac{F_F}{\dot{m}_0}$$

Razão de Empuxo

$$FR = \frac{\frac{F_F}{\dot{m}_0}}{\frac{F_C}{\dot{m}_0}}$$



Consumo específico

$$S = \frac{f}{(1 + \alpha) F / \dot{m}_0}$$

Eficiências (*conferir*)

$$\eta_t = \frac{a_0^2 \left[(1 + f) \left(\frac{V_9}{a_0} \right)^2 + \alpha \left(\frac{V_{19}}{a_0} \right)^2 - (1 + \alpha) M_0^2 \right]}{2f h_{PR}}$$

$$\eta_p = \frac{2M_0 \left[(1 + f) \frac{V_9}{a_0} + \alpha \frac{V_9}{a_0} - (1 + \alpha) M_0 \right]}{\left[(1 + f) \left(\frac{V_9}{a_0} \right)^2 + \alpha \left(\frac{V_{19}}{a_0} \right)^2 - (1 + \alpha) M_0^2 \right]}$$

$$\eta_o = \eta_p \eta_t$$